THE PERFORMANCE OF CACHE-BASED
ERROR RECOVERY IN MULTIPROCESSORS

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Abstract

Several variations of cache-based checkpointing for rollback error recovery in shared-memory multiprocessors have been recently developed. By modifying the cache replacement policy, these techniques use the inherent redundancy in the memory hierarchy to periodically checkpoint the computation state. Three schemes, different in the manner in which they avoid rollback propagation, are evaluated in this paper. By simulation with address traces from parallel applications running on an Encore Multimax shared-memory multiprocessor, we eva'uate the performance effect of integrating the recovery schemes in the cache coherence protocol. Our results indicate that the cache-based schemes can provide checkpointing capability with low performance overhead but uncontrollable high variability in the checkpoint interval.

Keywords. Fault-tolerant computing, cache-based checkpointing and rollback recovery, shared-memory multiprocessors, trace-driven simulation.

1 Introduction

In fault-tolerant computing systems checkpointing and rollback are often used to allow recovery from detected errors without a global restart of computation. Even under adverse conditions, most of the computation cycles in a typical system are error-free. It is therefore important to minimize the overhead of the error recovery mechanisms. Cache-based checkpointing is a hardware approach to user-transparent checkpointing from transient errors [10]. It uses the inherent redundancy in the memory hierarchy for maintaining checkpoints. The technique has been extended to shared-memory multiprocessors by integrating the checkpointing and recovery algorithms with cache coherence protocols [1, 24].

This paper presents an analysis of the impact on system performance for several variations of cache-based error recovery in bus-based multiprocessors. Simulation with address traces from an Encore Multimax shared-memory parallel processor is employed to gather statistics on the performance of the memory hierarchy in multiprocessors with several variations of cache-based error recovery. These statistics are then used to derive the overall system performance impact.

Several techniques have been proposed to provide rollback recovery in general-purpose architectures. Some commercial machines have implemented the capability to retry an instruction if an error is detected during execution [8]. Tamir and Tremblay proposed micro rollback, a generalization of instruction retry that supports rolling back execution a number of clock cycles by delaying writes to the register file and cache and backing up individual state registers [23]. Li *et al.* showed that the register delayed write buffer can be eliminated by using compiler techniques to preserve the state of a register for the desired number of cycles [15]. Instruction retry schemes have the disadvantages that processors can only roll back a few cycles, and that modifications have to be made in the processor design.

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Bowen and Pradhan recently developed a scheme that supports checkpointing and recovery at a higher level, in the virtual memory translation hardware [6]. Before a memory page is modified, a backup copy is made. The overhead of this scheme due to an increase in page manipulations can be made small by making the checkpoint interval large. Trace-driven simulations have shown an overhead of less than 1% for a checkpoint interval of 1 million memory references [6]. The scheme requires modification of the microprocessor TLB.

The use of a cache to save the checkpoint state was first proposed by Lee *et al.* [14]. Their recovery cache simply stores all data that are part of the checkpoint state and that have been overwritten in memory. Every write to a memory location must be preceded by a read to that location to maintain the data in the recovery cache. The original cache-aided rollback error recovery (CARER) scheme for uniprocessors, proposed by Hunt and Marinos [10], does not require an extra cache for checkpointing and adds no extra read cycles. It modifies the replacement policy of the regular cache to prevent replacement of dirty data, thereby keeping a checkpoint state in main memory. When dirty data lines need to be replaced, a checkpoint has to be taken. Wu *et al.* extended this scheme to shared-memory parallel processors [24]. To prevent rollback propagation, the source processor is also checkpointed immediately after it has communicated with another processor. Ahmed *et al.* presented two alternative algorithms for multiprocessors [1]. In one of the schemes, checkpointing is fully synchronized to occur at the same time on all processors. In a modification of this simple scheme, a checkpoint on one processor induces concurrent checkpoints on all processors that have had any communication activity since the previous checkpoint. Algudady *et al.* have also extended Wu's scheme to multistage interconnection networks [2].

Hunt and Marinos evaluated their uniprocessor CARER technique by trace-driven simulation and found a modest performance overhead for small caches [10]. Until our work, the multiprocessor cache-based

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recovery methods had only been analyzed using estimates of the probabilities of various events. Wu *et al.* used analytical modeling to show that for certain workload and system parameters their scheme results in slight performance degradation, especially when a special buffer is used to store data lines needed only for checkpointing. Using the same approach, Ahmed *et al.* arrived at similar results for their recovery schemes. Algudady *et al.* used a queuing model to predict an overhead of 2 to 12% depending on the degree of sharing. The performance predicted with each of these models depends highly on the estimates of the probabilities of various cache events. In this paper, we actually measure the probabilities of the cache events by trace-driven simulation and use these probabilities to derive a more accurate and realistic measure of the performance impact of multiprocessor cache-based error recovery. In this paper we evaluate the performance of Wu's communication-induced scheme, and Ahmed's fully synchronized and flagged synchronized schemes.

2 Cache-Based Checkpointing in Multiprocessors

2.1 Description of Algorithms

In the CARER cache-based checkpointing proposal [10], a checkpoint is taken every time a dirty cache line is written back. The replacement policy for a set associative cache is modified so that a checkpoint is avoided by selecting clean lines for replacement whenever possible. At a checkpoint the internal processor registers are saved and all dirty lines in the cache are marked *unwritable*. Unwritable lines may be read, but have to be written back to memory before they are modified. When a rollback is necessary all cache lines except the unwritable lines are invalidated and the saved processor registers are restored, thereby restarting the computation at the last checkpoint. Since the checkpoint state is stored partially in the cache and partially in main memory, both should be highly reliable or protected by their own error detection and

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recovery mechanisms.

Multiprocessor systems present the problem of rollback propagation. A rollback of one processor may necessitate a rollback of other processors that have communicated with it. These extra rollbacks may in turn cause further rollbacks, resulting in a domino effect that may extend completely back to the beginning of execution [20]. In a shared-memory multiprocessor, communication occurs when a processor reads a variable that has been written by another processor. If cache-based checkpointing is used, only data that have been checkpointed are written back to main memory. Therefore, rollback propagation occurs only when data are moved directly between caches.

In a shared-memory multiprocessor that caches its synchronization variables, rollback propagation can be eliminated by checkpointing the source processor after every communication [24]. In this communication-induced scheme the destination processor is allowed to roll back past an interaction, which will not affect correctness unless the program uses a synchronization variable to order memory accesses. In that case the accesses to the synchronization variables in the cache automatically enforce the correct checkpointing.

Another way to avoid the domino effect is by limiting the amount of rollback propagation through fully synchronized checkpointing. A checkpoint on one processor immediately causes a checkpoint on all other processors. Similarly, a rollback on one processor causes all others to roll back to the last checkpoint.

An enhancement to this simple scheme, originally proposed by Ahmed et al., is flagged synchronized checkpointing and rollback [1]. We modify their algorithm slightly by allowing the receiver of a message to roll back past the interaction. Two flags are required in every cache controller. The R flag is set when a cache has received data since the last checkpoint. The S flag is set when a cache has sent data since the last checkpoint. A checkpoint on one processor raises the *establish checkpoint* bus line if its R flag is raised. Processors with S flags raised take a checkpoint upon sensing the *establish checkpoint* signal. Similarly, a
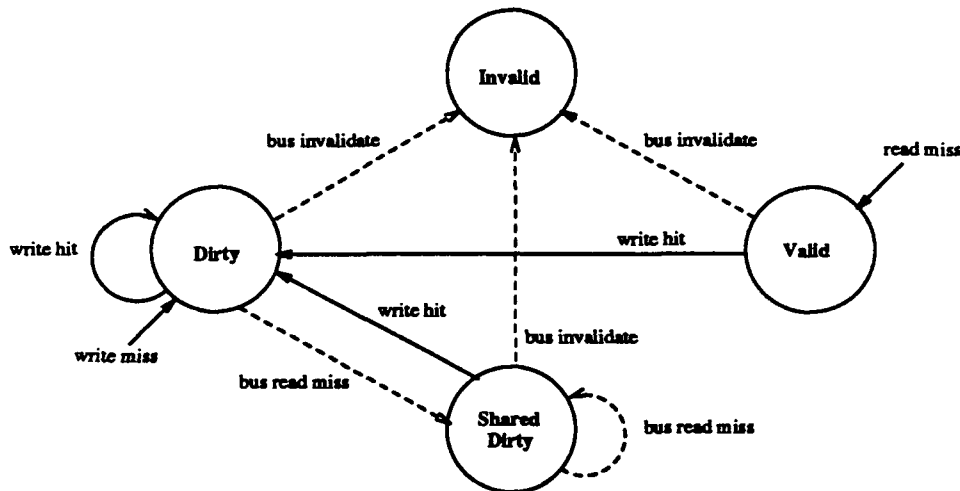
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Figure 2.1: The Berkeley cache coherence protocol.

rollback on a processor raises the *rollback* line if its *S* flag is set. Only processors with their *R* flags raised will actually take a checkpoint upon sensing the *rollback* signal.

The Berkeley write-invalidate coherence protocol [13] was used in this study. Figure 2.1 shows the transition diagram for the Berkeley protocol. To integrate the checkpointing schemes into the protocol, an *unwritable (owned)* and a *shared unwritable* state were added to the four original states of *invalid, valid, dirty (owned)*, and *shared dirty*. In the communication-induced checkpointing scheme, a bus miss on a dirty line will always cause a checkpoint, forcing the state into *shared unwritable*. Therefore, the *shared dirty* state is not needed. Figures 2.2 and 2.3 show the transition diagram for the modified Berkeley protocols.

2.2 Performance Impact

There are several ways in which cache-based checkpointing affects the overall performance of a computer system. For set associative caches, the modification of the LRU replacement policy affects the miss ratio. However, the effect of the replacement policy on cache miss ratio is generally small [9]. Also, the addition of an *unwritable* state affects bus traffic. At any time a certain percentage of the modified cache lines will be
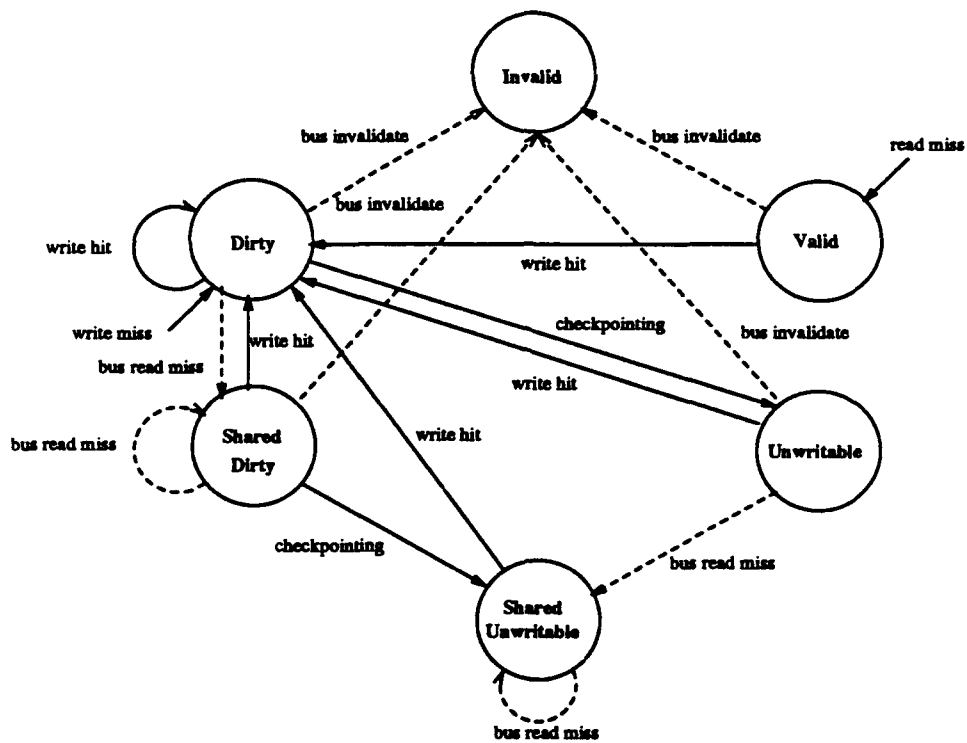
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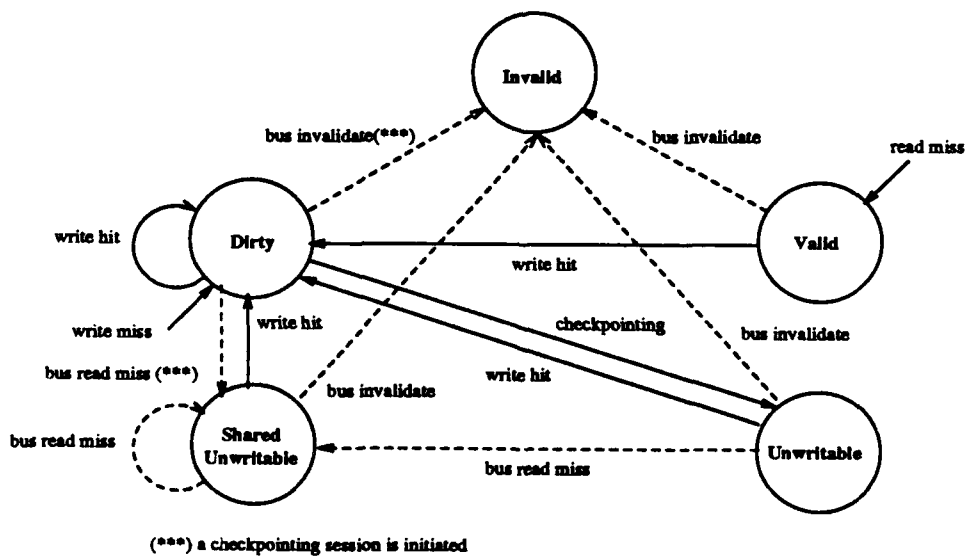Figure 2.2: Berkeley protocol modified for synchronized checkpointing schemes.

(***) a checkpointing session is initiated

Figure 2.3: Berkeley protocol modified for communication-induced checkpointing scheme.

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unwritable instead of *dirty*. On a write hit, an *unwritable* line has to be written back to main memory before it can be updated, causing a delay and extra bus traffic. In multiprocessors with a write-invalidate cache coherence protocol, the bus traffic is increased even further by the need to write back unwritable lines before they can be invalidated. In both cases, the data written back are checkpoint data; from the computation's point of view they have been overwritten. To eliminate the extra bus traffic, these data can be stored in a recovery buffer local to every cache [24].

The most direct effect on the performance of recoverable systems is created by the time needed to take checkpoints. This overhead increases both with the length and frequency of checkpointing events. If the internal processor state can be saved in one cycle and checkpoint indentifiers are used, the average time to take a checkpoint can be made less than two cycles [24]. However, the time to take a checkpoint may need to be increased to allow for error latency. Since the cache-based schemes can take checkpoints very quickly, relatively high checkpointing frequencies can be tolerated. The checkpointing frequency depends on the behavior of the program and the caches. Parts of the program that have consecutive writes to the same cache line will checkpoint frequently, to enable writeback of the dirty data. Increasing cache associativity increases the probability of finding a clean line to replace, thereby decreasing the number of necessary checkpoints.

In the communication-induced checkpointing schemes, program sections with high inter-cache communication, such as areas of contention for synchronization variables, will also have a high checkpointing frequency. The flagged synchronized scheme is much less sensitive to communication, since a checkpoints is only taken when a dirty cache line needs to be replaced. The fully synchronized scheme always induces checkpoints in all processors, so its performance is independent of the amount of communication, but always worse than that of the flagged scheme. Since checkpoints can occur in bursts, there may be sections

Table 3.1: Address traces used in the simulations.

program	description	static code size (instructions)	input	num. of cpus
gravsim	N-body simulator	6,985	two colliding 128-body clusters	7
tgen	test generator	16,179	ISCAS benchmark s208 w. 20 faults	7
fsim	fault simulator	13,451	ISCAS benchmark s208 w. 80 input vectors	7
pace	circuit extractor	16,101	two bit slices of an ALU	7
phigure	global router	19,046	469 cell circuit	7

programs where performance is significantly degraded. Therefore, the schemes may not be suitable if the program needs to meet real-time constraints.

3 Trace-Driven Simulation Experiments

3.1 Methodology and Workload

The address traces used in this study were generated by a version of the TRAPEDS address trace generator on the Encore Multimax shared-memory multiprocessor [11, 21, 22]. The interleaving of the processor traces in our experiments was determined by using the microsecond timer available on the Multimax. The traces were saved to disk and later fed into a multiprocessor recovery cache simulation.

The traces used were from five parallel C programs, written using Encore's standard parallel library, running on an eight-processor Multimax 510 [16]. The applications and inputs used to generate the traces are described in Table 3.1. Gravsim is a gravitational N-body simulator using the Barnes and Hut algorithm [3, 5]. Tgen is a test pattern generator for sequential and combinational circuits using a parallel search algorithm [19]. Fsim is a parallel fault simulator for digital circuits [19]. Pace is a parallel circuit extractor [4].

Table 3.2: Characteristics of the address traces.

program	tot. num. of references	data reads		data writes		code reads
		total	shared	total	shared	
gravsim	92,178,814	33,266,880	12,484,455	6,392,078	251,694	52,519,859
tgen	101,264,382	32,613,809	16,550,450	4,461,889	642,796	64,188,674
fsim	149,918,375	50,950,933	39,326,911	3,958,919	999,127	95,008,523
pace	87,861,165	23,266,576	1,286,787	7,842,338	348,524	56,752,251
phigure	132,998,231	38,244,233	4,281,207	11,530,981	1,876,400	83,223,027

Phigure is global router using structured hierarchical decomposition of independent tasks [7]. The amount of synchronization in each program varies. At one extreme, gravsim synchronizes repeatedly at barriers and has multiple critical sections. On the other hand, phigure does not use any barrier synchronization and has only one critical section.

All traces were generated on seven processors. The eighth processor was used to monitor the progress and disk usage of the trace. Table 3.2 describes the characteristics of the generated traces. The total number of memory references is separated into data reads, data writes, and code reads. All memory reference numbers are the total references from all seven processors. All applications were traced from beginning to end, resulting in traces of more than 10 million memory references per processor in every case.

3.2 Experimental Results

Simulations were performed using the Berkeley cache coherence protocol for the fully synchronized, flagged synchronized, and communication-induced checkpointing schemes. The versions of the flagged synchronized and communication-induced schemes simulated allow the receiver to roll back past an interaction. Cache sizes were varied from 4K to 256K bytes, while line size was held fixed at 16 bytes. Direct mapped, two-way set associative, and four-way set associative caches were simulated. Cache and checkpointing
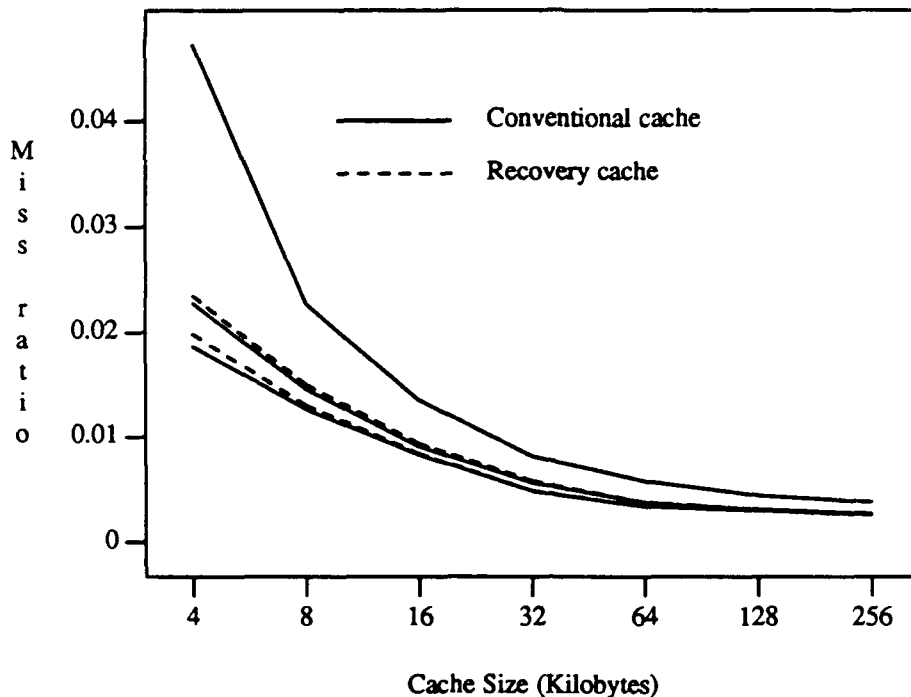
Figure 3.4: Miss ratios for direct mapped, two-way set associative, and four-way set-associative caches.

statistics were calculated on a per-processor basis and then averaged to arrive at a single number for each application.

As expected, the modified replacement policy used in the cache-based error recovery schemes has only a slight effect on the performance. The average miss ratios for the five programs are shown in Figure 3.4. The fraction of references that cause writebacks, the writeback ratio, is shown in Figure 3.5. In the direct mapped cache, the miss ratio and the base writeback ratio (traffic resulting from writebacks needed for the computation) remain the same. In the set associative caches, they vary by an insignificant amount with the modified replacement policy of the recovery schemes. The total number of writebacks consists of those needed for checkpointing in addition to the base writebacks. The frequency of these additional writebacks depends heavily on the frequency of checkpointing and will therefore be discussed after introducing the checkpointing frequency data.
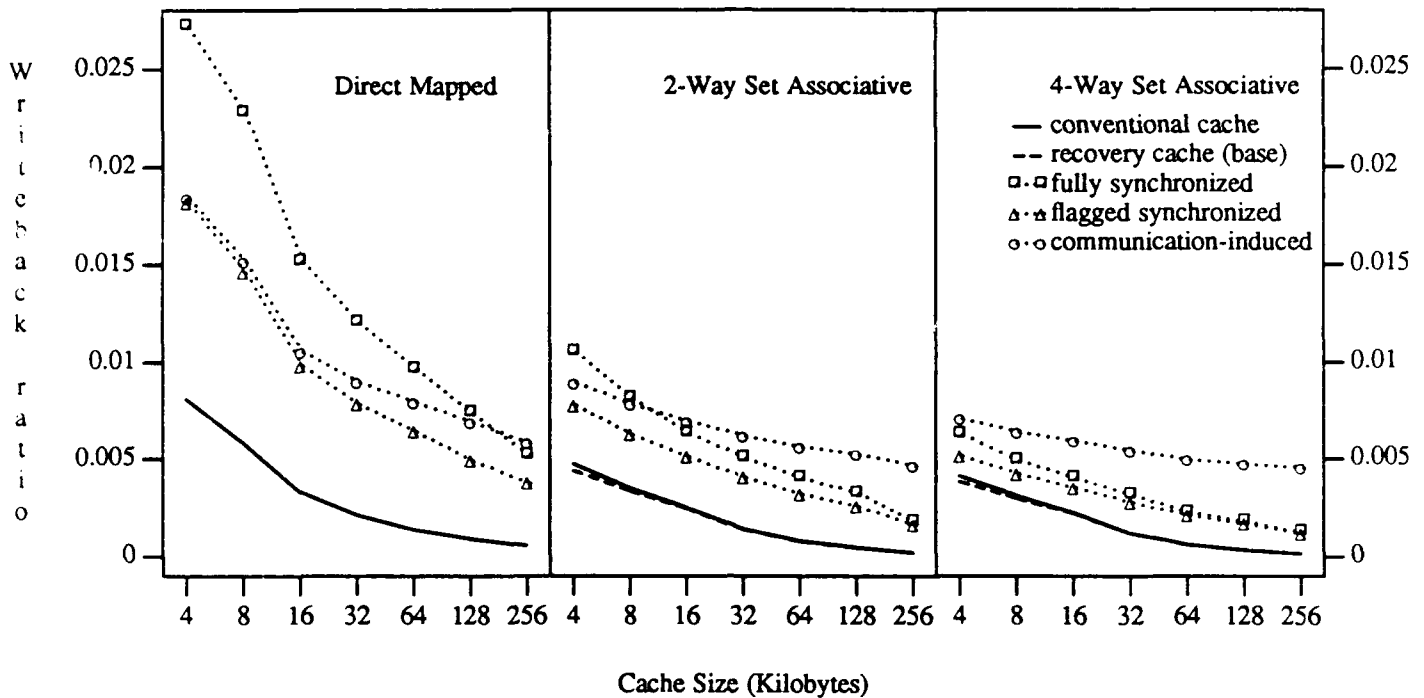
Figure 3.5: Writeback traffic.

Figure 3.6 presents, on a logarithmic scale, the average of the checkpointing frequencies for all the programs except phigure. The base checkpointing frequency includes all checkpoints that are taken due to the necessity of writing back a dirty cache line. The total checkpointing frequency also includes the checkpoints induced in other processors. The base checkpointing frequency decreases exponentially as cache size is increased; it decreases significantly as associativity is introduced. Figure 3.7 presents the checkpointing frequency for the phigure program, in which a large percentage of the data accesses are write accesses (see Table 3.2). The base checkpointing frequency for phigure is about an order of magnitude higher than for the other programs. In the two-way set associative cache the frequency decreases less than expected with cache size until it drops dramatically at 256 Kilobytes. This behavior is probably due to a few variables in the same cache set that are frequently modified and therefore need to be written back upon replacement, causing a checkpoint.
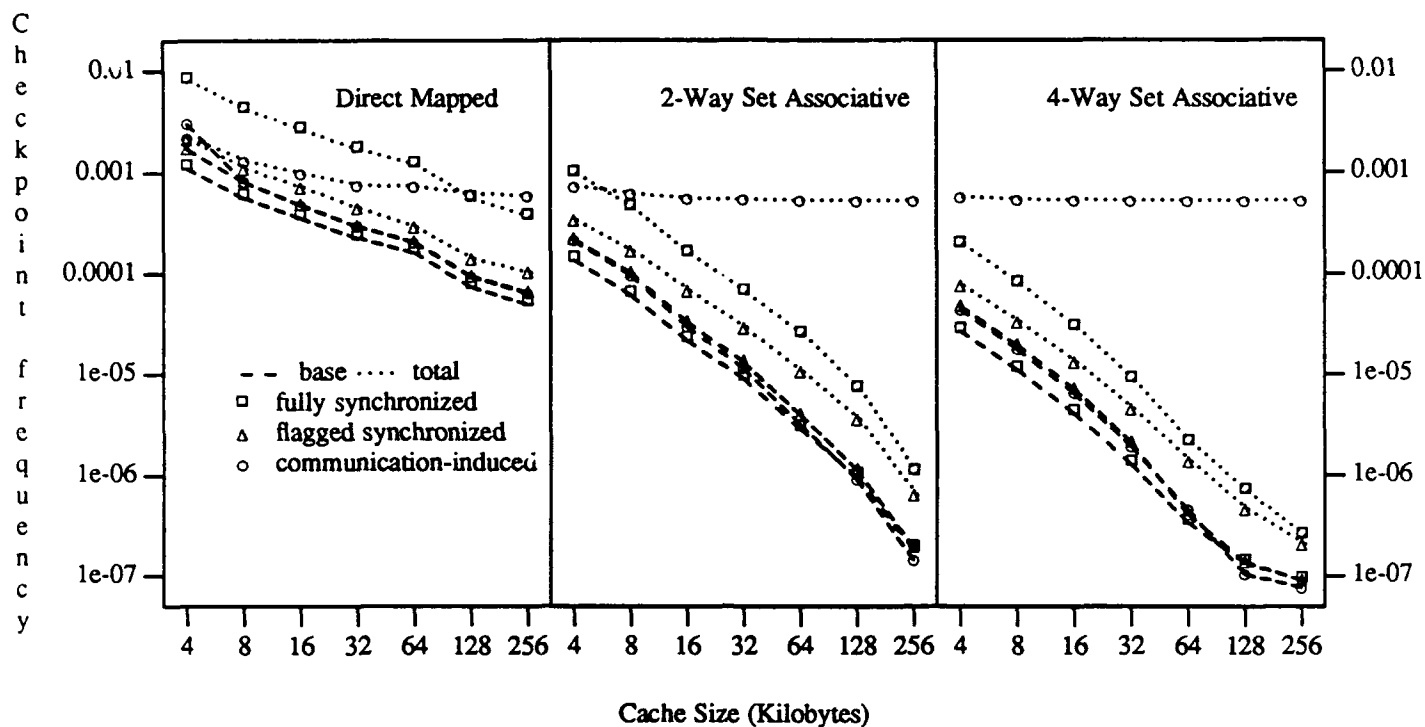
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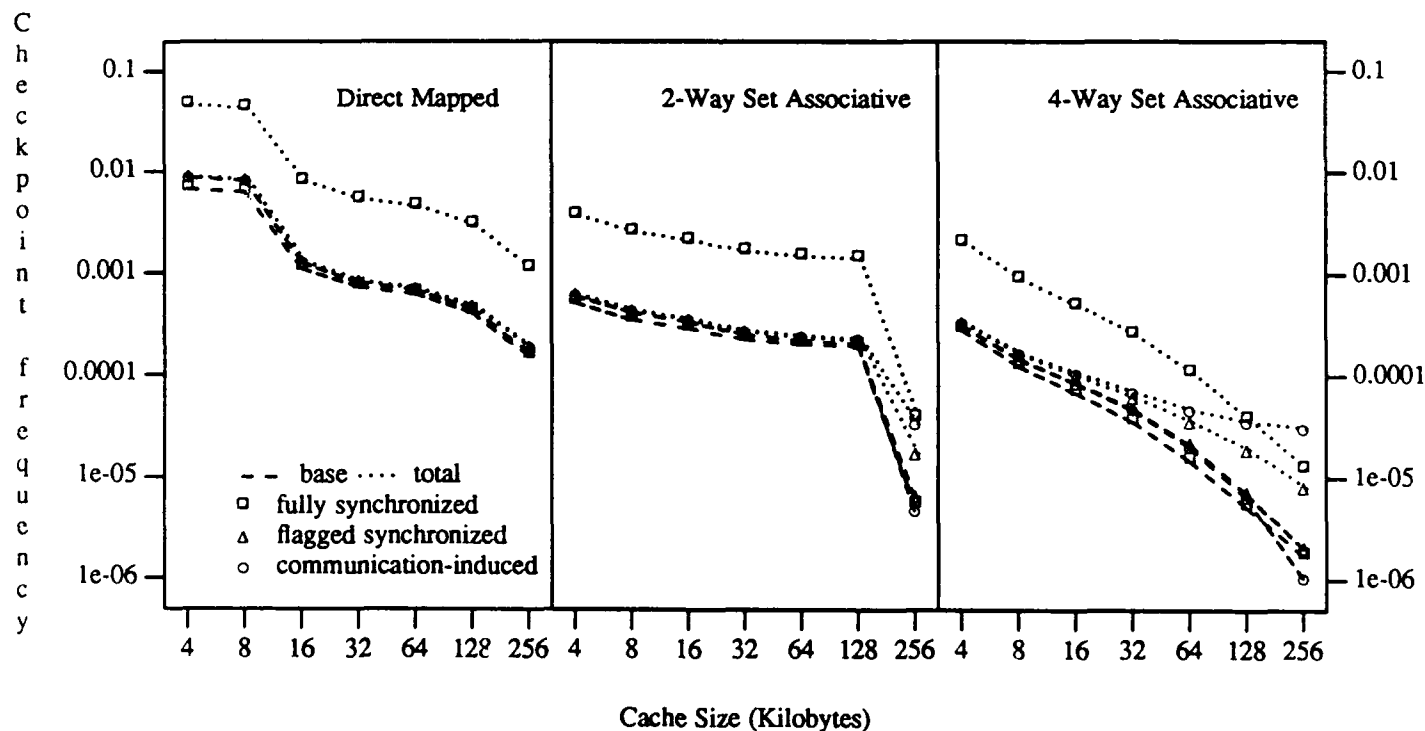Figure 3.6: Average checkpointing frequency for all programs except phigure.

Figure 3.7: Checkpointing frequency for phigure.

The extra induced checkpointing frequency varies with the recovery scheme used. In the fully synchronized scheme, a checkpoint on one processor causes simultaneous checkpoints on all other processors. Therefore, the total checkpointing frequency remains at approximately seven times the base frequency. The large number of induced checkpoints actually reduces the number of base checkpoints by clearing the cache frequently of dirty lines. The flagged synchronized scheme drastically reduces the induced checkpointing frequency, since checkpoints are induced only if communication has occurred with the originating processor. Even in programs with large amounts of communication, the flagged synchronized scheme performs much better than the fully synchronized scheme. In programs with little communication, the increase over the base checkpointing frequency is negligible. The number of extra checkpoints in the communication-induced scheme is fixed regardless of cache size. On average it performs well compared to the synchronized schemes only for small cache sizes. In the case of phigure, which has little communication, there are very few induced checkpoints, but the performance of the communication-induced scheme is still inferior to that of the synchronized schemes in large set associative caches.

In all three schemes, even when the average checkpointing frequency is low, there is no guaranteed minimum checkpointing interval. Figure 3.8 presents the average length of the checkpoint interval, along with the average length plus one standard deviation, the average length minus the standard deviation, the length of the largest interval, and the length of the smallest interval. In all cases, the smallest interval is of length zero, while the largest intervals are in the tens of millions of instructions. Under the communication-induced checkpointing scheme, all intervals are very small, regardless of cache size. In the synchronized schemes, increasing cache size increases the checkpoint interval. However, even in the largest cache there are still checkpoint intervals of zero accesses.

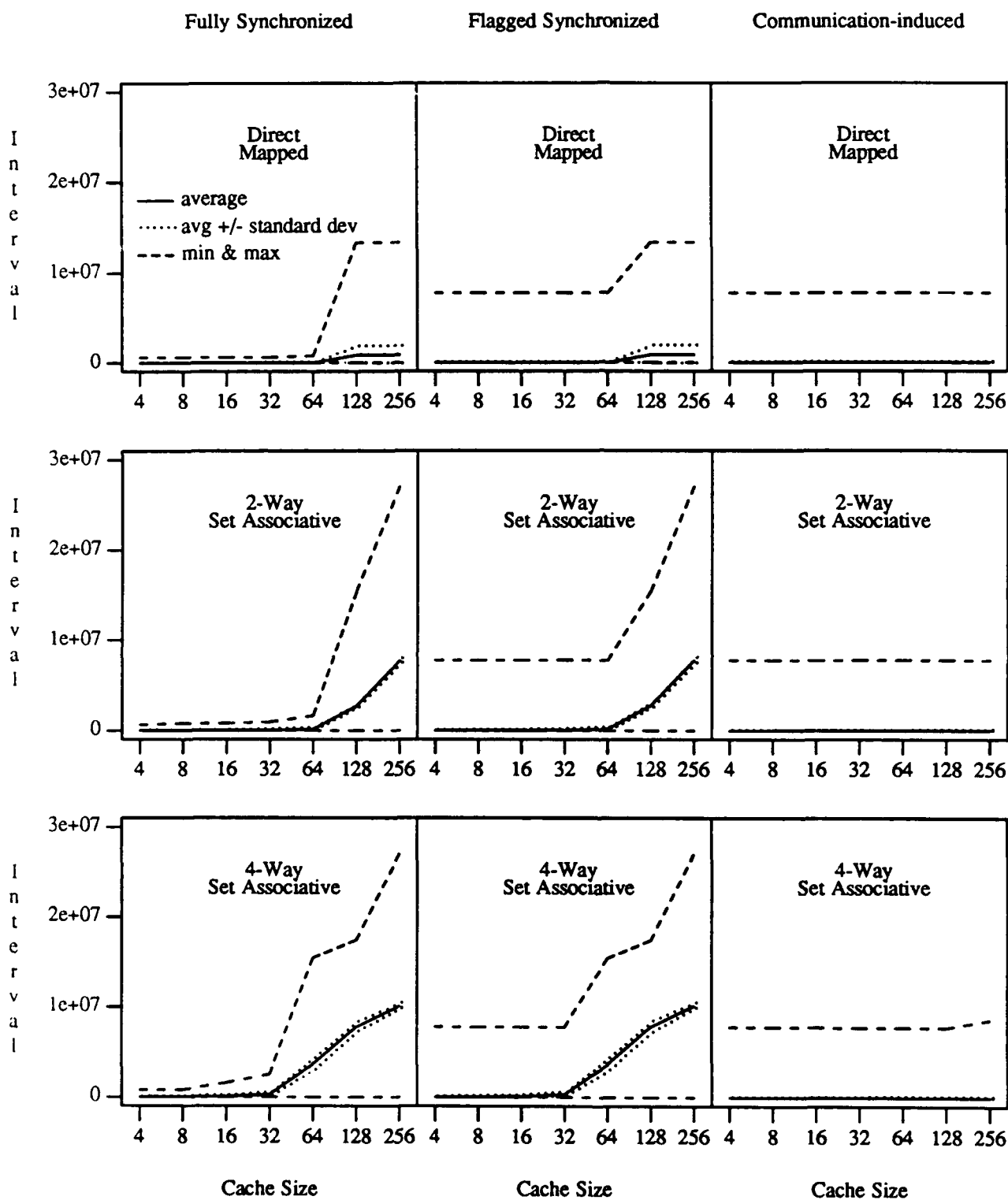The total writeback traffic is influenced by the checkpoint frequency. The chance of an extra writeback

Figure 3.8: Average and deviations for length of checkpoint interval.
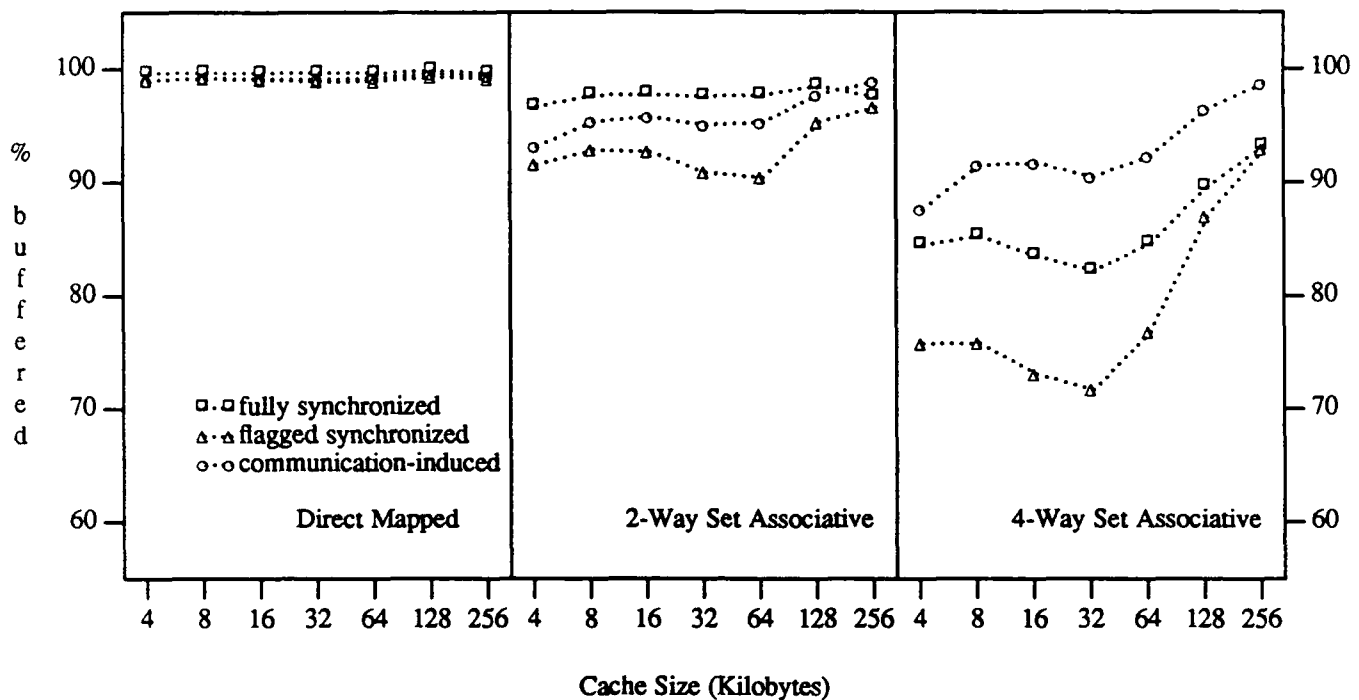
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Figure 3.9: Extra writebacks captured by a recovery buffer with 1/16th the capacity of the cache.

due to the modification or invalidation of an unwritable cache line is determined by the percentage of unwritable lines present in the cache. The more frequently checkpointing occurs, the more likely it is for a modified block to be in the unwritable rather than dirty state. A comparison of Figures 3.5 and 3.6 shows that the number of extra writebacks indeed increases with increased checkpoint frequency. The extra writeback frequency of the synchronized schemes shows variability with the cache size, while that of the communication-induced scheme does not, just as in the case of checkpoint frequency. The extra writebacks can easily double the total traffic. In large caches almost all of the traffic is due to extra writebacks.

Extra writebacks to main memory can be eliminated by storing the replaced unwritable lines in a buffer local to the cache, which is cleared at every checkpoint. If the buffer fills up before a checkpoint is taken, the writebacks proceed to the main memory. Figure 3.9 shows the percentage of extra writebacks that can be stored in a buffer with 1/16th the capacity of the cache. Since the checkpoint frequency is very high in direct

Table 4.3: Parameters generated from simulation using address traces.

Parameter	Description
N	number of processors (7)
m	miss ratio
w_b	base writeback ratio
w_x	extra writeback ratio due to write hits to unwritable lines
f_b	fraction of extra writebacks that go to recovery buffer
i	invalidate ratio: fraction of references that cause an invalidation
o	other cache ratio: fraction of references that cause data to be transferred from another cache
c	checkpoint frequency

mapped caches, nearly 100% of all writebacks can be stored in the recovery buffer. When checkpointing

is less frequent, the recovery buffer fills up more often. In all cache organizations, however, the recovery

buffer catches at least 70% of the extra writebacks in the traces simulated.

4 System Performance

4.1 Performance Model

The cache performance and checkpointing frequency figures generated from our address traces interact to

affect overall system performance. Their impact will vary with the specific architecture of the multiprocessor

system involved. However, it is instructive to determine the performance impact of supporting cache-based

error recovery in a typical multiprocessor. The performance metrics generated by the cache simulation were

used in a simple processor and bus behavior model similar to that developed by Patel [17, 18]. The model

consists of three equations, with three unknowns representing the actual execution time Z for one unit of

useful work, the bus utilization B, and the average waiting time W per bus request.

Table 4.4: Assumed parameters.

Parameter	Value used	Description
a	0.70	processor memory reference rate
T	4	number of cycles to transfer a cache line
I	4	number of cycles to invalidate a cache line
A	2	number of cycles for bus arbitration
R	2	number of cycles to store a cache line in the recovery buffer
C	varied	average number of cycles to take a checkpoint

Table 4.3 describes the parameters of the model that are generated directly from the trace-driven simulations. Other parameters depend on the specifics of the multiprocessor. Their description and assumed values are given in Table 4.4.

The performance model is described in the most general terms by assuming the cache has recovery capability and a recovery buffer. If recovery is not implemented, the equations can be used with $w_x = c = 0$. If there is no recovery buffer, $f_b = 0$. The model uses the variable b, the average number of bus requests per cycle:

$$b = ma + ia + (1 - f_b)w_x a ,$$

where ma represent the bus requests due to cache misses, ia the bus requests due to invalidates of shared lines in other caches, and $(1 - f_b)w_x a$ the bus requests due to extra writebacks not caught by the recovery buffer.

The execution time Z for one unit of useful work is

$$Z = 1 + bA + maT + [w + (1 - f_b)]aT + iaI + bW + f_b w_x aR + caC + Q . \tag{1}$$

It includes one cycle to do the actual work and overheads of bA for bus arbitration, maT for cache misses, $[w + (1 - f_b)]aT$ for writebacks not caught by the recovery buffer, iaI for invalidations, bW for bus wait time, $f_b w_x aR$ for writes to the recovery buffer, caC for taking checkpoints, and Q for cache interference. Cache

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interference occurs when memory requests collide with invalidation or transfer requests. It is calculated as

$$Q = \frac{a(ia + oaT)}{1 + bA + bW} .$$

The average bus utilization B can be calculated two ways. The probability that no processor is requesting the bus is the unit request rate as seen from the bus subtracted from one and then raised to the power of the number of processors. The bus utilization B is in turn one minus this quantity, or

$$B = 1 - \left(1 - \frac{z - 1 - bA - f_b w_x aR - caC - Q}{Z}\right)^N . \tag{2}$$

The bus utilization can also be derived by multiplying N by the actual bus time used by a processor, and averaged over the execution period.

$$B = \frac{N(z - 1 - bA - f_b w_x aR - caC - bW - Q)}{Z} . \tag{3}$$

4.2 Performance Results

To compare the performance of the varying recovery cache scheme with a conventional cache, we define the percentage overhead associated with the memory system as

$$O = 100(1 - Z) .$$

In a perfect system with no cache misses, O would equal zero; in a real cache-based system O represents the percentage increase in execution time over such a perfect system.

Figure 4.10 presents the overheads for the recovery schemes without a recovery buffer and with the average checkpoint penalty $C = 2$. Overheads of over 20% are not shown to allow increasing the scale of the graphs. Even in small direct mapped caches, the additional overhead of the checkpointing schemes is never higher than a few percent. The communication-induced scheme performs badly in caches that are
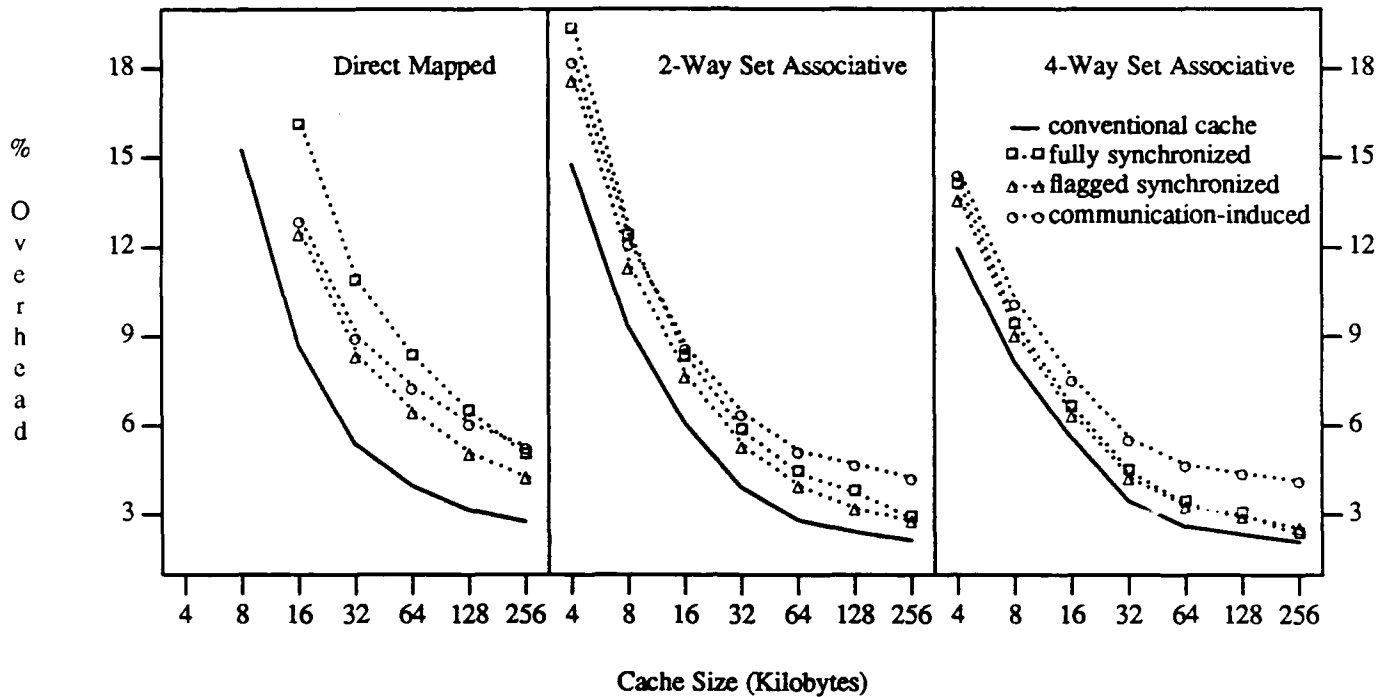
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Figure 4.10: Performance overhead without recovery buffer, $C = 2$.

large or have high associativity. The fully synchronized scheme performs badly in caches that are small or have low associativity. The flagged synchronized schemes performs the best in all cases.

Addition of a recovery buffer greatly improves the performance, especially when checkpoint intervals are small. Figure 4.11 presents the overhead for the recovery schemes with a recovery buffer with 1/16th the capacity of the cache. With the recovery buffer, all schemes only increase the overhead by a few percentage points from that of the conventional cache. Even though the flagged synchronized scheme still performs best, its comparative advantage is reduced.

An average checkpoint penalty of 2 cycles may not be realistic in some systems. It may be impossible to save the internal processor state in one cycle. It may also be necessary to insert a delay of a number of cycles before a checkpoint to allow for error latency. Figure 4.12 presents the overheads with a recovery buffer when the average checkpoint penalty C is increased to 100. With the high checkpoint penalty,
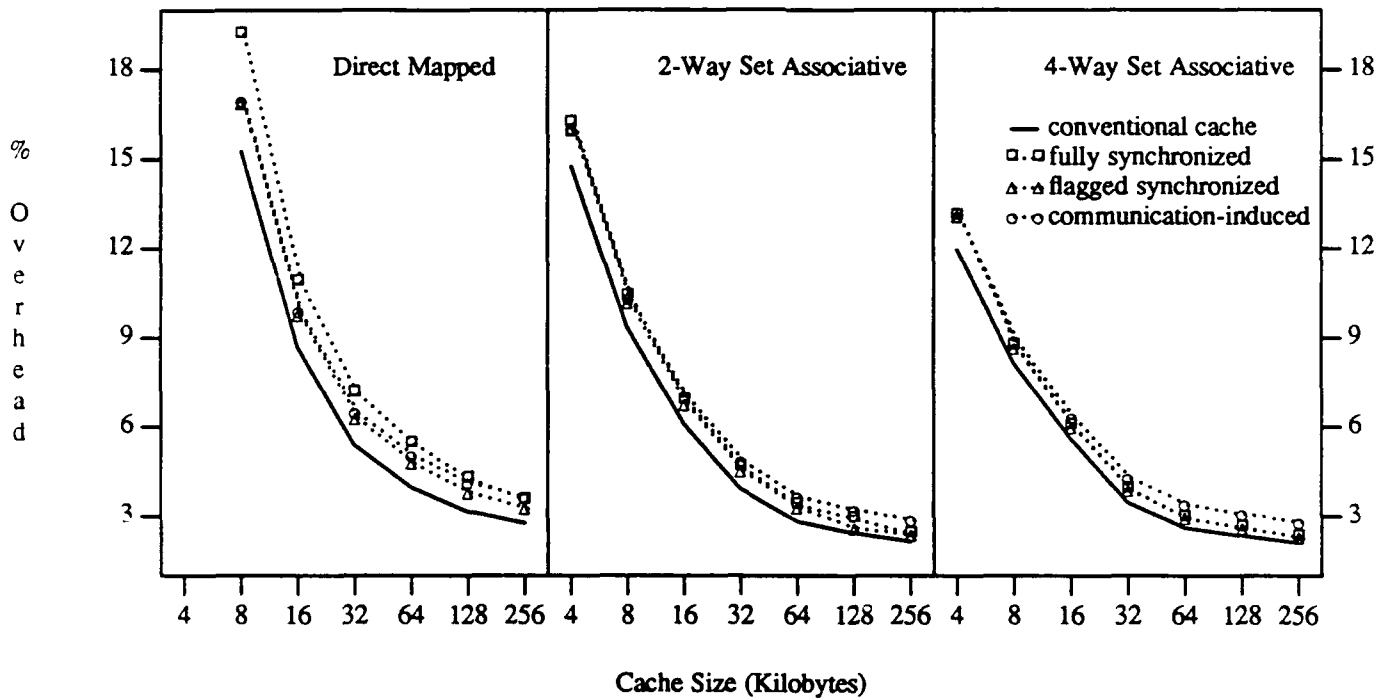
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Figure 4.11: Performance overhead with recovery buffer, $C = 2$.

the overhead increases noticably where checkpoint frequency is high. The communication-induced and fully synchronized schemes are affected the most by the higher checkpoint penalty, whereas the flagged synchronized scheme is affected by a much smaller amount. In the set associative caches, the additional overhead of flagged synchronized checkpointing over a conventional cache is still less than one percent.

5 Conclusions

Trace-driven simulation was used to measure the performance of cache-based error recovery in a shared-memory multiprocessor. The results answer many questions that remained unresolved after previous approximate analytical performance studies of the cache-based recovery methods. The cache miss ratio is not degraded by the addition of the recovery scheme to the cache protocol. The writeback traffic increases
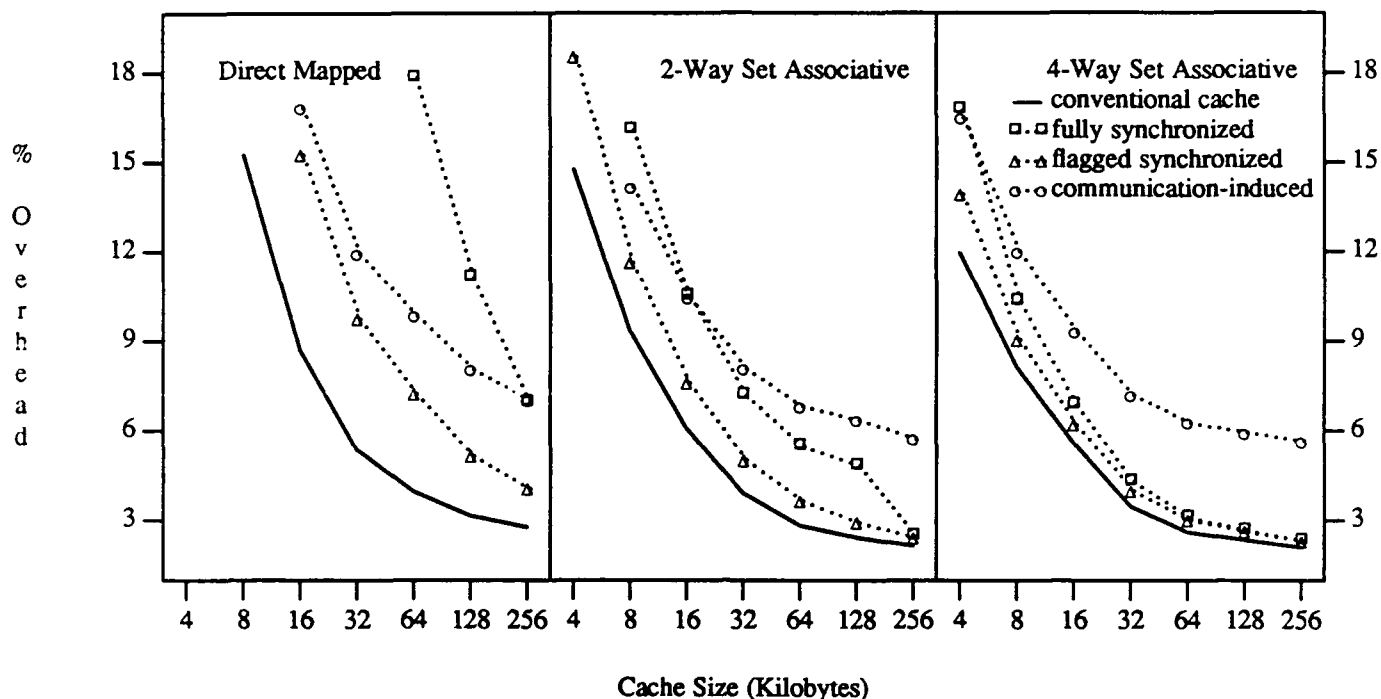
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Figure 4.12: Performance overhead with recovery buffer, $C = 100$.

significantly. However, a recovery stack at every cache can intercept many of the extra writebacks caused by the recovery schemes.

The addition of cache-based recovery degrades performance by at most a few percent. The communication-induced scheme does not improve as cache size and associativity is increased. In the range of cache sizes used today, its performance compares unfavorably with that of the other schemes. The fully synchronized schemes works well only in large caches with high associativity. At the cost of extra cache hardware, the flagged synchronized scheme outperforms both other schemes in all cases. Its performance degradation is lowest in highly associative caches. But even in a two-way set associative cache with a high checkpoint penalty it degrades performance by one percent or less.

A major disadvantage of all the cache-based recovery schemes is the uncontrollability and variability of the checkpoint frequency as seen in the programs traced. This instability manifests itself both between

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different programs and within the execution length of a program. The performance of a system with cache-based checkpointing will therefore be less predictable than that of a system without recovery capability, even though average overhead is minimal. Future research should be directed at finding low-cost methods that eliminate this disadvantage.

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